

# Subtraction of DC Conductivity and Annealing: Approaches To Identify Johari–Goldstein Relaxation in Amorphous Trehalose

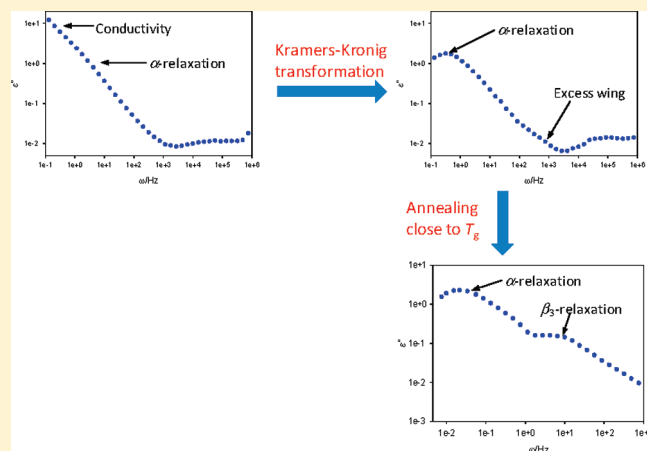
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**S** Supporting Information

**ABSTRACT:** Amorphous trehalose finds extensive use as a stabilizer of biomolecules including proteins and phospholipids. Hypothesizing that molecular mobility is a determinant of its stability, dynamic dielectric spectroscopy (DDS) was used to map the different modes of mobility. Isothermal dielectric relaxation profiles of amorphous trehalose were obtained, over the frequency range of  $10^{-1}$ – $10^7$  Hz, and at temperatures ranging from 30–170 °C. At temperatures close to the glass transition ( $T_g$ ), the  $\alpha$ -relaxation was not readily discernible due to interference from dc conductivity. We used Kramers–Kronig transformation that enabled not only the complete resolution of  $\alpha$ -relaxation but also the identification of an excess wing, in the high frequency tail of  $\alpha$ -relaxation. On annealing, this excess wing developed into a partially resolved and hitherto unidentified  $\beta$ -relaxation peak. This peak, due to its position in the dielectric spectrum, its annealing time dependence and the good agreement with the calculated independent relaxation time, was assigned to the Johari–Goldstein process. This work demonstrates the utility of conductivity subtraction coupled with sub- $T_g$  annealing to successfully study all the modes of mobility in amorphous trehalose. This approach can potentially be extended to situations wherein dc conductivity impedes the complete characterization of molecular mobility.

**KEYWORDS:** trehalose, dielectric spectroscopy, molecular mobility, Kramers–Kronig, annealing, Johari–Goldstein relaxation



## INTRODUCTION

In light of the very poor aqueous solubility of numerous drug candidates under development, amorphization is increasingly emerging as a possible strategy for solubility enhancement.<sup>1</sup> However, the increased free energy of an amorphous compound, when compared with its crystalline counterpart, can also result in decreased physical stability, manifested by the tendency to crystallize. Molecular mobility, an extensively studied property of amorphous materials, can be a major determinant of stability.<sup>2,3</sup> A correlation between global molecular mobility (i.e.,  $\alpha$ -relaxation) and physical stability has been documented in many amorphous materials.<sup>4–6</sup> Therefore, a reduction in molecular mobility has often been suggested as a strategy for improving physical stability. Recently, several studies have shown the possible role of secondary relaxations in the physicochemical stability of amorphous materials. Local mobility involves fast noncooperative motions arising from the orientation of individual molecules or their parts.<sup>7–9</sup> These local motions are also referred to as  $\beta$ -relaxations. Evidence of crystallization at temperatures far below  $T_g$  and crystallization tendencies not explained by structural relaxation time are two indirect observations which have strongly hinted at the importance of local mobility.<sup>10–13</sup> Although there can be many secondary relaxations, often the slowest

$\beta$ -relaxation, referred to as the Johari–Goldstein (JG) relaxation, has received the most attention in literature.<sup>14,15</sup> In addition to its potential role in governing stability, JG relaxation may also be a precursor to global mobility.<sup>16,17</sup>

Many instrumental techniques such as differential scanning calorimetry (DSC),<sup>18,19</sup> dielectric spectroscopy,<sup>4,5</sup> shear viscosity measurement<sup>20</sup> and nuclear magnetic relaxation time measurement<sup>6,21</sup> have been employed to study molecular mobility in amorphous materials. Dynamic dielectric spectroscopy (DDS) is a technique that enables a “mapping” of the different modes of mobility over a wide range of temperatures.<sup>22,23</sup> It offers unique advantages in that it not only can distinguish between local and global mobility but can even differentiate one secondary relaxation from another. In fact, it has been the most successful technique to study secondary relaxations in a variety of materials.<sup>9,11,14,15,24</sup> One major drawback, as was found in many sugars and polyalcohols, is the contribution of ionic or dc conductivity to the imaginary part of complex permittivity or dielectric loss.<sup>25,26</sup> This can potentially

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interfere with the characterization of  $\alpha$ -relaxation, if both occur in the same frequency region.<sup>24,25</sup> In such situations, there are two possible approaches to analyze the underlying relaxation. If the  $\alpha$ -relaxation peak is discernible as a shoulder in the steep conductivity, the Havriliak–Negami model which takes into consideration both relaxation and dc conductivity can be used to fit this region of dielectric spectrum (eq 1).

$$\varepsilon^*(\omega) = \left[ \varepsilon_\infty + \frac{\Delta\varepsilon}{(1 + (i\omega\tau)^{\beta_{\text{HN}}})^{\gamma_{\text{HN}}}} \right] + \frac{\sigma_0}{i\varepsilon_s\omega} \quad (1)$$

$$\varepsilon^*(\omega) = \varepsilon'(\omega) - i\varepsilon''(\omega) \quad (2)$$

where  $\varepsilon^*(\omega)$  is the complex dielectric permittivity comprising of a real part  $\varepsilon'(\omega)$  and an imaginary part  $\varepsilon''(\omega)$ ,  $\omega$  is the frequency,  $\tau$  is the relaxation time,  $\sigma_0$  is the dc conductivity and  $\Delta\varepsilon$  is the dielectric strength given by  $(\varepsilon_s - \varepsilon_\infty)$ , where  $\varepsilon_s$  is the static permittivity or the low frequency limit ( $\omega \rightarrow 0$ ) of  $\varepsilon'(\omega)$  and  $\varepsilon_\infty$  is the high frequency limit ( $\omega \rightarrow \infty$ ) of  $\varepsilon'(\omega)$ .  $\beta_{\text{HN}}$  is a parameter describing symmetric peak broadening with  $0 < \beta < 1$  while  $\gamma_{\text{HN}}$  is the asymmetric broadening parameter with  $0 < \gamma < 1$ .

However, in light of the potentially serious errors due to fitting, such an approach has not found widespread use. The second possible strategy is to use the Kramers–Kronig relation or the so-called Hilbert transform.<sup>25–27</sup> This relation links the real (dielectric constant,  $\varepsilon'$ ) and the imaginary (dielectric loss,  $\varepsilon''$ ) parts of the complex dielectric permittivity  $\varepsilon^*$ . If the dielectric constant is known at two frequencies ( $\omega_1$  and  $\omega_2$ ), one can calculate the dielectric loss at the median frequency (logarithmic scale) using the derivative form of the Kramers–Kronig relation (eq 3). When there is no contribution of interfacial polarization to the permittivity, the dielectric constant has contributions only from relaxation processes. In such cases, only dc conductivity contributes to dielectric loss.

$$\varepsilon'' \approx \frac{\pi}{2} \frac{\varepsilon'(\omega_1) - \varepsilon'(\omega_2)}{\ln\left(\frac{\omega_2}{\omega_1}\right)} \quad (3)$$

Trehalose ( $\alpha$ -D-glucopyranosyl  $\alpha$ -D-glucopyranoside) finds extensive use as a stabilizer of biomolecules including proteins and phospholipids.<sup>28,29</sup> This protective property is believed to be due to its rigid glassy state and its ability to act as a “water substitute”.<sup>30</sup> Accordingly, the amorphous form of trehalose has been the subject of many investigations. It exhibits many interesting properties including a high glass transition temperature ( $T_g \sim 117^\circ\text{C}$ ) and relatively low crystallization tendency. However, recently, crystallization of trehalose was observed during freeze-drying.<sup>31,32</sup> Since the amorphous state is a necessary (though not sufficient) condition for its ability to serve as a bioprotective and a stabilizer, its crystallization behavior warrants serious investigation.

Molecular mobility in amorphous trehalose, our compound of interest, has received only limited attention in the literature.<sup>24,25,33–35</sup> Because of the conductivity interference, until recently,  $\alpha$ -relaxation in trehalose could not be monitored by dielectric spectroscopy, at temperatures close to  $T_g$ . Earlier this year, based on fitting the dielectric loss data, Kwon et al. reported four relaxations in amorphous trehalose.<sup>36</sup> Since the dc conductivity was not subtracted, there is room for ambiguity in data interpretation.<sup>25</sup> Given its importance as a widely occurring bioprotective, there exists an urgent need to comprehensively study the molecular mobility of amorphous trehalose. By effectively subtracting out the

contribution of dc conductivity, we have demonstrated the ability to completely resolve  $\alpha$ -relaxation even at sub- $T_g$  temperatures. This subtraction, coupled with annealing, also enabled the identification of an excess wing, attributable to JG relaxation. This laid the foundation for the complete mapping of molecular mobility, encompassing the  $\alpha$ - and several  $\beta$ -relaxations.<sup>37</sup>

## EXPERIMENTAL SECTION

**Preparation of Amorphous Trehalose.** Trehalose dihydrate ( $\text{C}_{12}\text{H}_{22}\text{O}_{11} \cdot 2\text{H}_2\text{O}$ ; Sigma, St. Louis, MO, USA; purity >99%) was used as received. Freeze-dried trehalose was obtained by lyophilization in a benchtop freeze drier (model UNITOP 400 L, Virtis, Gardiner, NY, USA). About 15 mL of aqueous trehalose solution (10% w/v) was placed in Petri dishes, cooled to  $-45^\circ\text{C}$ , and subjected to reduced pressure (100 mTorr). After holding the sample for 2 min at  $-45^\circ\text{C}$ , the temperature was slowly increased to  $-30^\circ\text{C}$  and primary drying was carried out for 38 h. Over the next 24 h, the temperature was gradually increased to  $50^\circ\text{C}$ . The secondary drying was carried out at  $50^\circ\text{C}$  for 31 h, after which the temperature was raised to  $60^\circ\text{C}$  and the drying continued for 24 more hours. The samples were removed from the freeze-drier, transferred to glass containers, tightly capped and stored in a desiccator at  $-20^\circ\text{C}$  over anhydrous calcium sulfate (RH < 5%) until use. Further handling of the freeze-dried samples was done in a controlled humidity environment (<5% RH; in a glovebox).

**Baseline Characterization of Amorphous Trehalose.** Amorphous trehalose prepared by freeze-drying was found to be X-ray amorphous with a water content <0.5% w/w (determined by Karl Fischer titrimetry and thermogravimetry), and a calorimetric  $T_g$  of  $\sim 117^\circ\text{C}$  (onset temperature).

**Dynamic Dielectric Spectroscopy.** Dielectric constant and dielectric loss measurements were performed with a broadband dielectric spectrometer (Novocontrol Alpha-A high performance frequency analyzer, Novocontrol Technologies, Germany). About 100 mg of sample was placed between two round copper electrodes (20 mm diameter) and a PTFE spacer. The PTFE spacer (thickness, 1 mm; area, 59.69 mm<sup>2</sup>; capacity, 1.036 pF) was used to keep the sample confined between electrodes at high temperatures and also to minimize errors due to stray capacitance or edge effects. To study different relaxations, the dielectric measurements were carried out isothermally at various temperatures, from 30 to  $170^\circ\text{C}$ , typically in the frequency range of  $10^{-1}$  to  $10^7$  Hz. The sample temperature was maintained with a Novotherm temperature controller.

**Analysis of Dielectric Relaxation Spectroscopy Data.** The basic model describing a dielectric process is the Debye function, which considers a symmetric dielectric loss peak with a constant full width at half-maximum value of 1.14 decades. However, in most cases, the peaks of dielectric materials are much broader and often asymmetric. The Havriliak–Negami function (eq 1 but without the conductivity term) can be used to describe the symmetric and asymmetric broadening of the relaxation peaks.

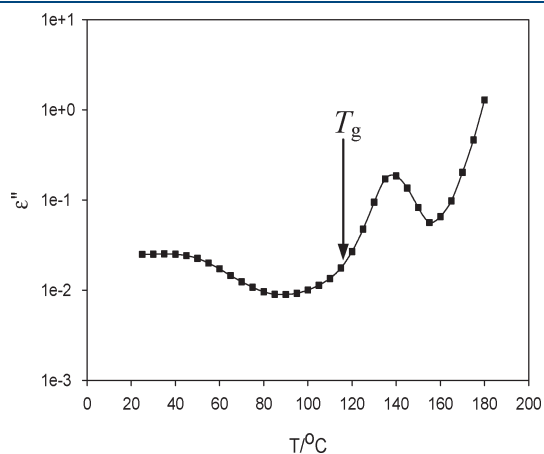
## RESULTS AND DISCUSSION

In order to examine the general dielectric features attributable to molecular motions in the glassy and supercooled melt of trehalose,  $\varepsilon''$  and  $\varepsilon'$  were determined at a fixed frequency of 1 kHz, typically in temperature increments of  $5^\circ\text{C}$ , over the range of  $25$ – $180^\circ\text{C}$  (temperature sweep experiment). Figure 1 is a plot of  $\varepsilon''$  as a function of temperature, at a fixed frequency of 1 kHz. The

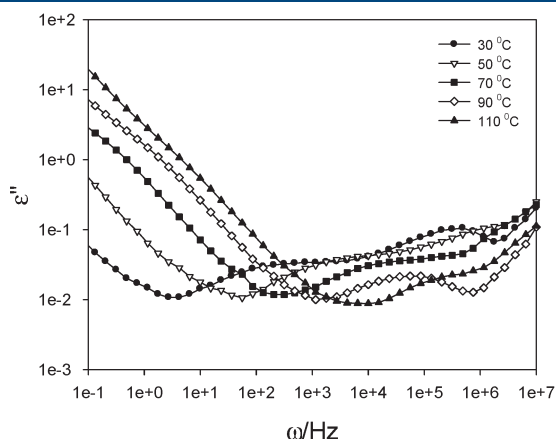
calorimetric  $T_g$  onset is indicated in the figure. On heating through the  $T_g$ ,  $\epsilon''$  rapidly increased, reached a maximum and then decreased. This peak is attributed to  $\alpha$ -relaxation, the major contributor to dielectric permittivity. Additionally, an extra “contribution” on the low temperature tail of the  $\alpha$ -relaxation peak and a peak at  $\sim 40^\circ\text{C}$  were observed, both attributed to two secondary relaxations. Thus, the temperature sweep experiment indicated at least three relaxations in the investigated temperature range.

Isothermal frequency sweep experiments were also conducted in the temperature range of  $30$ – $170^\circ\text{C}$ . The frequency range employed was  $10^{-1}$ – $10^7$  Hz, and the time for each measurement was  $\sim 5$  min. As the temperature was increased, at low frequencies, there was an increased contribution of dc conductivity to the dielectric loss (Figure 2).

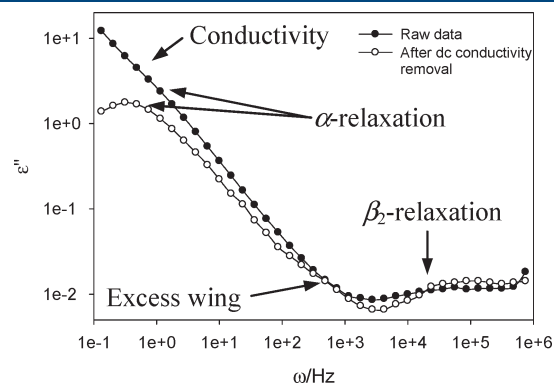
Figure 3 is a plot of the  $\epsilon''$  as a function of frequency, obtained at  $100^\circ\text{C}$ . The peak in the frequency range of  $10^4$ – $10^5$  Hz has been attributed to  $\beta_2$ -relaxation.<sup>24,35</sup> From the raw  $\epsilon''$  profile (filled circles),  $\alpha$ -relaxation can be barely discerned as a curvature (pointed out in the figure) in the steeply rising region of dc conductivity. As already mentioned, earlier investigations had also pointed out this limitation.<sup>24,25,34,35</sup> We attempted to overcome this problem using the Kramers–Kronig relation at temperatures both above and below  $T_g$ . The  $T_g$  was determined to be  $\sim 120^\circ\text{C}$  based on the change in temperature dependence



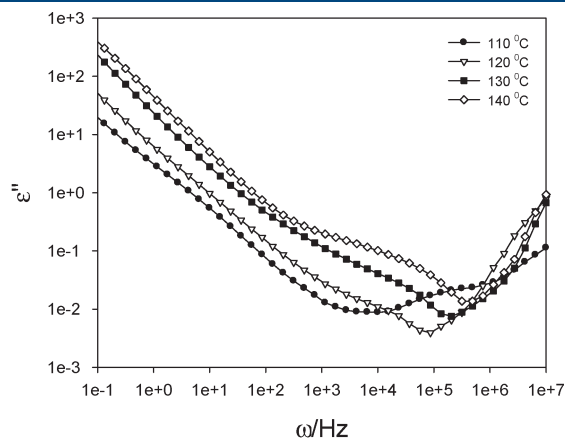
**Figure 1.** Plot of dielectric loss versus temperature in amorphous trehalose. The calorimetric  $T_g$  onset is shown by an arrow.



of  $\alpha$ -relaxation. It was possible to use the Kramers–Kronig relation since there was no contribution of interfacial polarization to the real part of dielectric permittivity (Figure 4; the small increase at low frequencies is attributed only to  $\alpha$ -relaxation). This enabled us to calculate, over the entire frequency range, the dielectric loss values from dielectric constant data, thereby effectively eliminating the contribution of dc conductivity and completely resolving the  $\alpha$ -relaxation peak (open circles in Figure 3). It is however recognized that the differential form of the Kramers–Kronig relation is an approximation and has some limitations.<sup>38</sup> The Havriliak–Negami model was used to fit the peak and obtain the average relaxation time and shape parameters (Table 1). Interestingly, an excess wing was observed on the high frequency tail of the  $\alpha$ -relaxation peak. When the experiments were conducted at several temperatures close to but  $< T_g$ , the excess wing persisted. However, this feature vanished at temperatures  $> T_g$  (addressed later). In an earlier report, Kaminski et al. had effectively used the Kramers–Kronig relation to investigate  $\alpha$ -relaxation in trehalose.<sup>25</sup> Since their studies were limited to the supercooled liquid phase, there was no reference to the excess wing. Recently, Kwon et al. have also reported an excess wing in the dielectric profile of trehalose.<sup>36</sup> However, their results were obtained by fitting the dielectric loss



**Figure 3.** Dielectric loss profile of amorphous trehalose at  $100^\circ\text{C}$ . Both raw  $\epsilon''$  profile (filled circles) and profile calculated using the Kramers–Kronig relation (open circles) are shown. Contribution from conductivity,  $\alpha$ -relaxation and  $\beta_2$ -relaxation is indicated by arrows. After the removal of dc conductivity interference,  $\alpha$ -relaxation can be clearly observed. A high frequency excess wing to the  $\alpha$ -relaxation is also apparent.

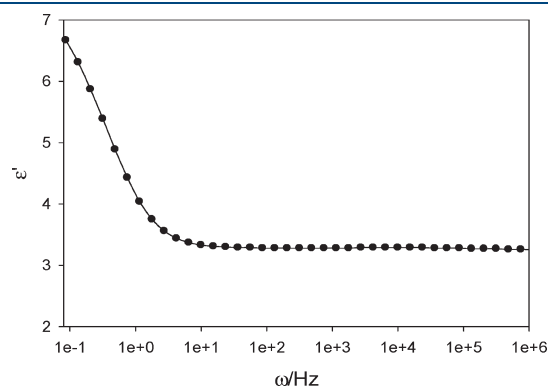


**Figure 2.** Isothermal dielectric profiles of amorphous trehalose over the temperature range of  $30$ – $140^\circ\text{C}$ . The contribution of dc conductivity increases at low frequencies as the temperature is increased.

data but without subtracting the contribution of dc conductivity. In light of the pronounced contribution of the conductivity, both in the regions of  $\alpha$ -relaxation and excess wing, unambiguous modeling of the relaxation data cannot be accomplished.

This excess contribution to the high frequency region of the  $\alpha$ -relaxation is a common feature in many glass formers, and has even served as a basis of classification of glass formers.<sup>39</sup> Type A glass formers are characterized by an excess wing without a well resolved  $\beta$ -relaxation, while type B glass formers exhibit a well-defined  $\beta$ -relaxation. Initially, there was a debate about the origin of this excess wing.<sup>39–43</sup> It was later shown, both in glycerol and in propylene carbonate, that the excess wing was indeed the high-frequency flank of the JG relaxation hidden under the  $\alpha$ -relaxation peak.<sup>42,43</sup> In both the compounds, on annealing, the excess wing developed into a shoulder indicating the presence of a secondary relaxation. Due to the inability of earlier studies to observe this excess wing, trehalose was implied to be a type B glass former.<sup>24,35</sup> Moreover, on separate occasions,  $\beta_1$ - and  $\beta_2$ -relaxations were identified as the JG relaxation.<sup>24,25,34</sup> The observation of an excess wing in amorphous trehalose is potentially important. It shows, in addition to the two  $\beta$ -relaxations already known, the existence of another  $\beta$ -relaxation. The JG relaxation, involving the motion of the whole molecule, is invariably the slowest of the secondary relaxations. In the dielectric spectrum, since this excess wing occurred between  $\alpha$ -relaxation and the already known secondary relaxations, it is hypothesized to be the JG relaxation (Figure 3). JG relaxation is believed to be a universal feature of amorphous materials and has often been viewed as a precursor to global mobility.

To completely characterize this excess wing, amorphous trehalose was annealed at 100 °C (17 °C <  $T_g$ ). The isothermal

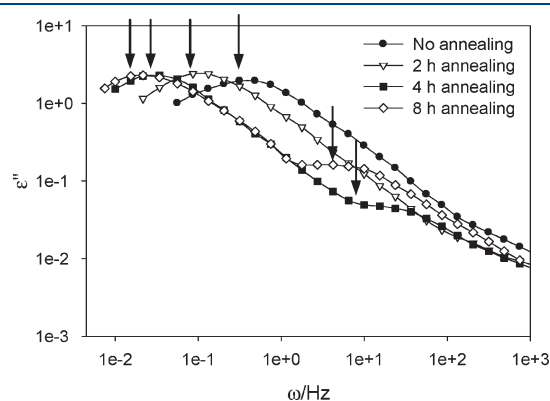


**Figure 4.** Dielectric constant of amorphous trehalose (at 100 °C) as a function of frequency.

dielectric profiles of samples annealed for different time periods are shown in Figure 5. Annealing for 2 h caused a pronounced shift in the  $\alpha$ -relaxation to lower frequencies. In addition, the excess wing developed into a shoulder. Further annealing ( $\geq 4$  h) facilitated the partial resolution of this hidden relaxation peak, which we termed  $\beta_3$ -relaxation. In trehalose, this resolution is much better than that observed in glycerol and propylene carbonate.<sup>42,43</sup> This partial separation enabled the use of the Havriliak–Negami model to fit the data and obtain the average relaxation time and shape parameters for this relaxation (Table 1). A representative dielectric spectrum of amorphous trehalose annealed for 8 h is shown in Figure 6. Lines represent the fitted profiles using the Havriliak–Negami model.

The  $\beta_3$ -relaxation peak could not be observed once the sample was heated above  $T_g$ . Heating above  $T_g$  erased the thermal history of the sample, thereby removing the effect of annealing. We had earlier pointed out that the excess wing in the unannealed trehalose could not be observed at temperatures above  $T_g$ . This is probably due to  $\alpha$ -relaxation exhibiting much more pronounced temperature dependence than  $\beta_3$ -relaxation.

It is apparent from the profiles of amorphous trehalose samples annealed for 4 and 8 h that  $\beta_3$ -relaxation peak increased in dielectric strength as trehalose was annealed although no such effect was seen on  $\alpha$ -relaxation (Figure 5). However, annealing for a much longer time (up to 120 h), caused an increase in the dielectric strength of  $\alpha$ -relaxation as well (data not shown). Thus, while the dielectric strength of both  $\beta_3$ - and  $\alpha$ -relaxations increase with annealing, the time required to exhibit this effect is



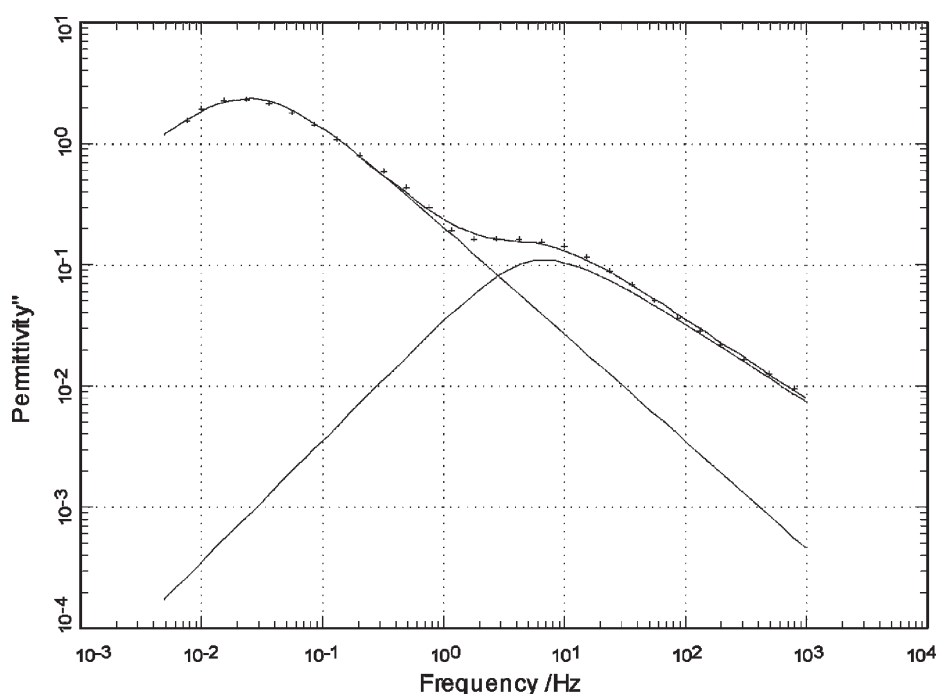
**Figure 5.** Isothermal dielectric relaxation profiles of different annealed samples of amorphous trehalose at 100 °C. The frequency of maximum dielectric loss ( $\omega_{\max}$ ) is shown by arrows for the two relaxations in different samples.

**Table 1.** Relaxation Time for the  $\alpha$ - and Different  $\beta$ -Relaxations in Amorphous Trehalose

	at 100 °C	at $T_g$ (~120 °C)
	Unannealed Sample	
$\alpha$ -relaxation time (s)	0.5	0.1
	Sample Annealed for 8 h at 100 °C	
$\beta_3$ -relaxation time (s)	$1.2 \times 10^{-2}$	$7.3 \times 10^{-3}$
Calculated independent relaxation time ( $\tau_0$ ) (s) <sup>a</sup>		$3.7 \times 10^{-3}$
$\beta_2$ -relaxation time (extrapolated value) (s)		$8.7 \times 10^{-8}$
$\beta_1$ -relaxation time (extrapolated value) (s)		$1.2 \times 10^{-8}$

<sup>a</sup> Note that the calculated independent relaxation time ( $\tau_0$ ; from the extended coupling model) at  $T_g$  is close to  $\beta_3$ -relaxation time, but is orders of magnitude longer than  $\beta_1$ - and  $\beta_2$ -relaxation times.





**Figure 6.** Isothermal dielectric relaxation profile of amorphous trehalose annealed for 8 h at 100 °C. Both  $\alpha$ - and  $\beta_3$ -relaxations are simultaneously fitted using the Havriliak–Negami model to obtain the average relaxation time and shape parameters.

very different. On the other hand, the frequency of maximum loss ( $\omega_{\max}$ ) very quickly shifted to lower values (i.e., longer relaxation time) for  $\alpha$ -relaxation, while this effect was just discernible (the  $\omega_{\max}$  values for the 4 and 8 h of annealing time are pointed out in Figure 5) for the  $\beta_3$ -relaxation peak. Thus qualitatively, annealing has a similar effect on both  $\beta_3$ - and  $\alpha$ -relaxations, suggesting that  $\beta_3$  is the true JG relaxation. In light of the potential importance of this observation, the effect of annealing time will be the subject of a separate publication.

Ngai proposed an extending coupling model, wherein JG relaxations (also referred to as independent relaxations) are considered as precursors to  $\alpha$ -relaxation.<sup>16</sup> The two relaxations are related by a temperature independent “crossover time”,  $\tau_c$ . At times shorter than  $\tau_c$ , JG relaxations are prevalent, and at times longer than  $\tau_c$ , these are transformed into the slower cooperative  $\alpha$ -relaxation. For most amorphous glass formers,  $\tau_c$  is  $\sim 2$  ps.<sup>17,44,45</sup> In an effort to further check if  $\beta_3$ -relaxation is the JG relaxation, the independent relaxation time,  $\tau_0$ , was calculated for the 8 h annealed sample using the coupling model by Ngai:<sup>16,17</sup>

$$\tau_0 = \tau_{\alpha}^{\beta_{\text{KWW}}} \times \tau_c^{(1 - \beta_{\text{KWW}})} \quad (4)$$

where  $\tau_{\alpha}$  is the  $\alpha$ -relaxation time at  $T_g$  and  $\beta_{\text{KWW}}$  is the measure of the deviation from exponential decay of the  $\alpha$ -relaxation time in the Kohlrausch–Williams–Watts (KWW) equation. Both were calculated from the experimentally obtained  $\alpha$ -relaxation parameters (see Supporting Information).<sup>46</sup> This was done to compare the calculated value of  $\tau_0$  with the experimentally determined value of  $\beta_3$ -relaxation at  $T_g$  (Table 1). The sample annealed for 8 h proved to be ideal for this purpose since the  $\beta_3$ -relaxation was sufficiently resolved. The  $\beta_1$ - and  $\beta_2$ -relaxation times at  $T_g$  calculated using the Arrhenius equation (see Supporting Information), were much shorter than  $\tau_0$ , indicating that neither of them correlated to  $\alpha$ -relaxation (Table 1). On the

other hand, the calculated value of  $\tau_0$  and the measured value of  $\beta_3$ -relaxation at  $T_g$  were in good agreement establishing the relationship of this secondary relaxation with the cooperative  $\alpha$ -relaxation, and supporting our hypothesis that it is the JG relaxation.

In summary, at temperatures below but close to  $T_g$ , subtraction of dc conductivity permitted not only the resolution of  $\alpha$ -relaxation but also the identification of an excess wing in the dielectric spectrum of amorphous trehalose. Annealing, at a temperature close to  $T_g$ , resulted in the development of this excess wing into an unresolved relaxation peak which could be successfully analyzed to determine its relaxation parameters. This relaxation peak, due to its position in the dielectric spectra, its similarity in annealing time dependence to  $\alpha$ -relaxation, and its good agreement with the calculated independent relaxation time, could be assigned to the JG process.

This work shows that, in order to successfully identify all the mobility features in the dielectric spectra, it is necessary to unambiguously study the relaxation profiles of amorphous materials at different temperatures. In case of disaccharides where there is considerable interference from dc conductivity, annealing coupled with the Kramers–Kronig approach could be very successful in identifying hidden but potentially important relaxation modes. This approach enabled the identification of JG relaxation, which can be of great practical importance in light of its potential impact on the stability of amorphous compounds.

## ■ ASSOCIATED CONTENT

**S Supporting Information.** Calculation of the extrapolated values of  $\beta_1$ - and  $\beta_2$ -relaxation times at  $T_g$  and calculation of the independent relaxation time from the  $\alpha$ -relaxation peak. This material is available free of charge via the Internet at <http://pubs.acs.org>.

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